



# NERO GRAV

New Refined Observations of Climate Change from Spaceborne Gravity Missions

International Spring School

Neustadt an der Weinstraße, Germany, March 10-14, 2025

## Mass Change of the Oceans

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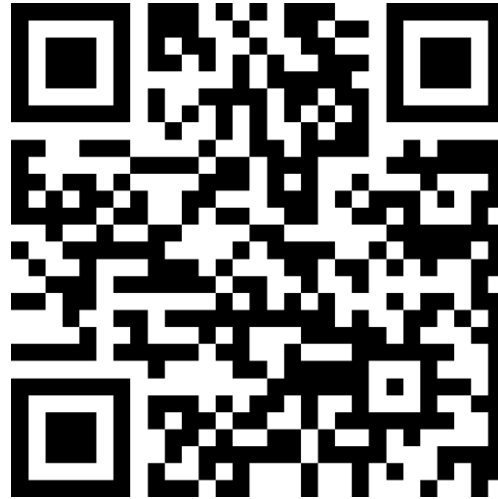


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# Mass Change of the Oceans

**Warm-up:**



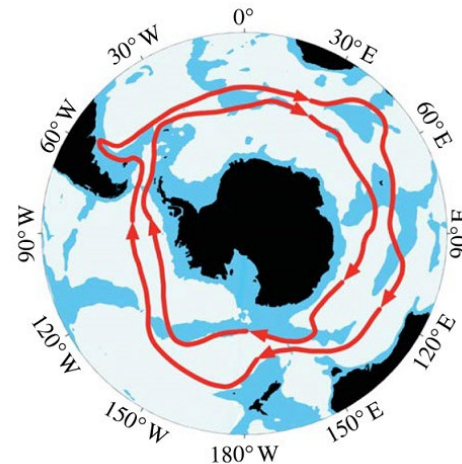
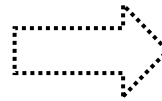
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# Mass Change of the Oceans

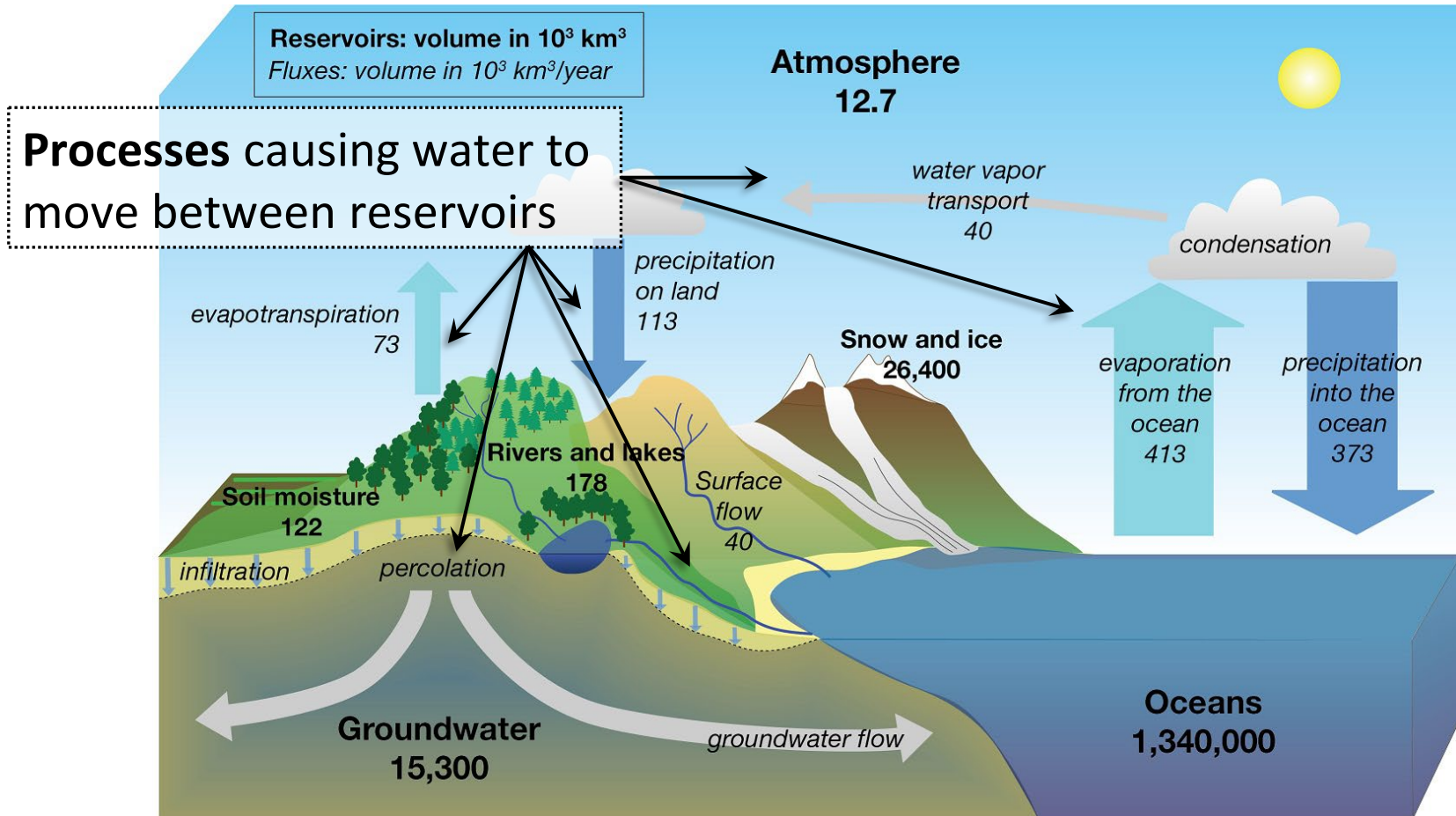
## Outline:

1. Basic considerations – hydrological cycle
2. Land-ocean mass transfer
3. Dynamic ocean
4. Ocean bottom pressure



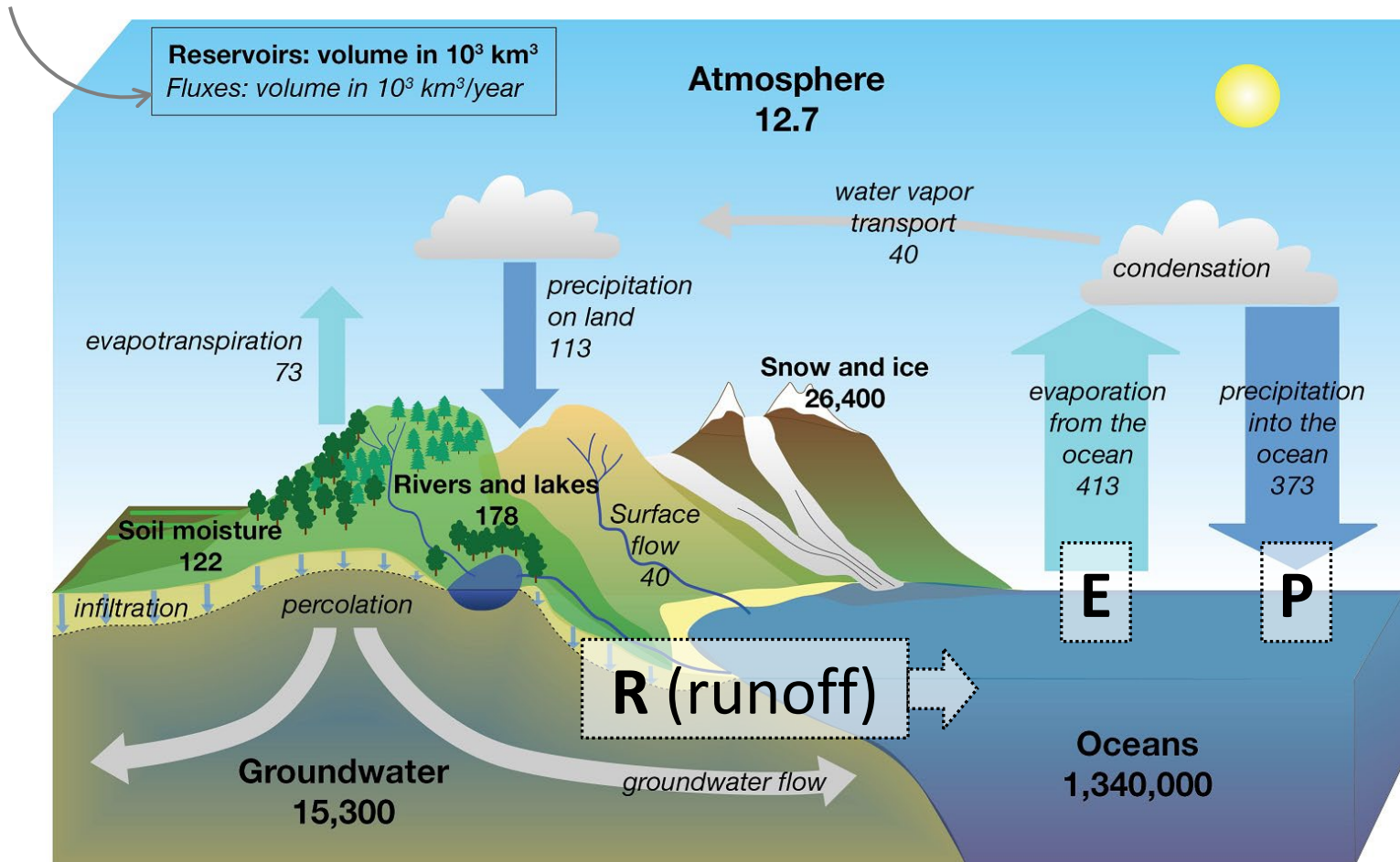
# Basic Considerations

## Ocean is integral to the hydrological cycle:



# Basic Considerations

*Fluxes* ... sum of transferred water over a nominal year



# Basic Considerations

## Water balance in the ocean:

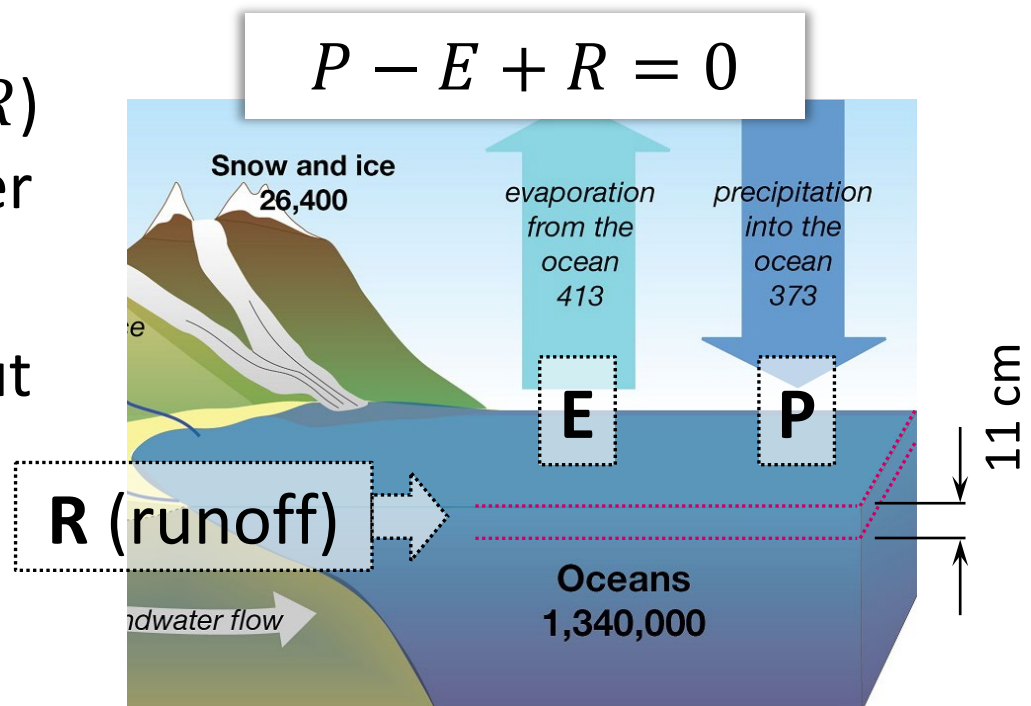
units:  $mm\ yr^{-1}$

	$P$	$E$	$P - E$	$R$	$P - E + R$
Global	1066	1176	-110	110	0

- Net fluxes ( $E - P$  or  $R$ ) evenly spread out over ocean  $\Rightarrow$  11-cm layer
- What goes in, goes out



**No change in  
ocean mass**

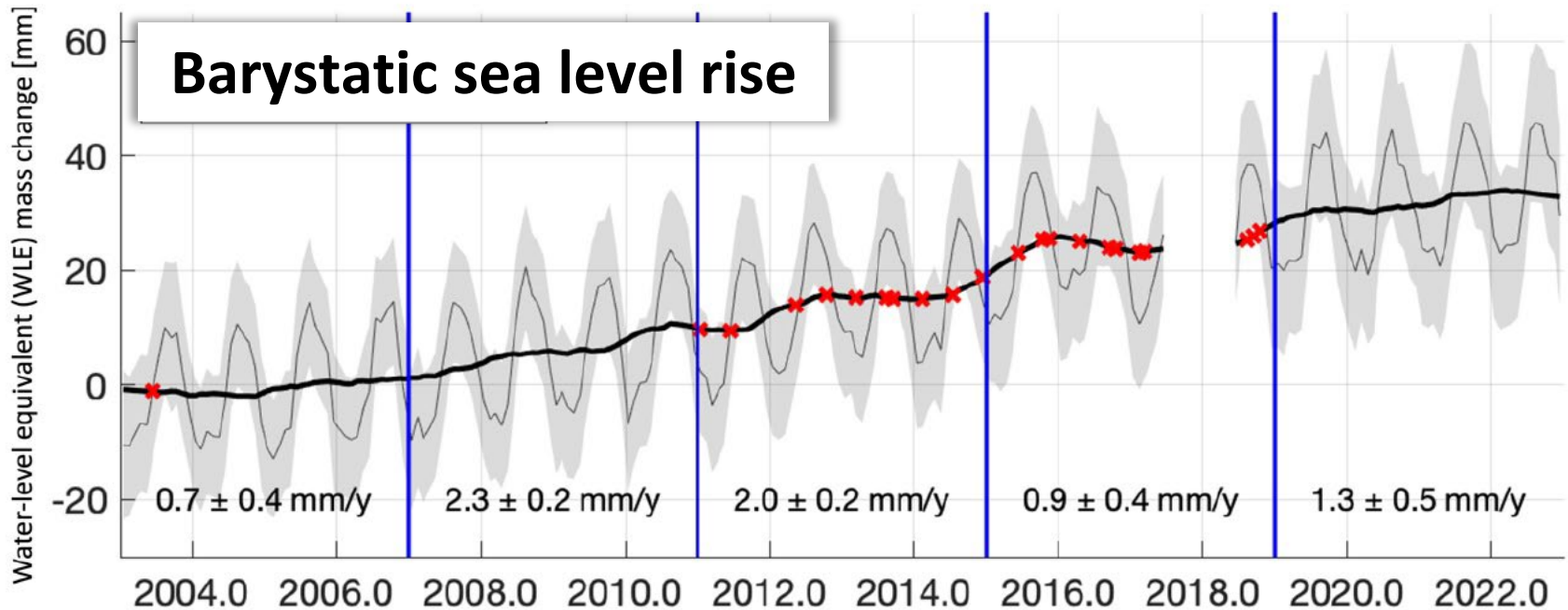




# Basic Considerations

## What does GRACE/-FO tell us?

Ocean mass increase  $\Leftrightarrow$  Imbalance of fluxes



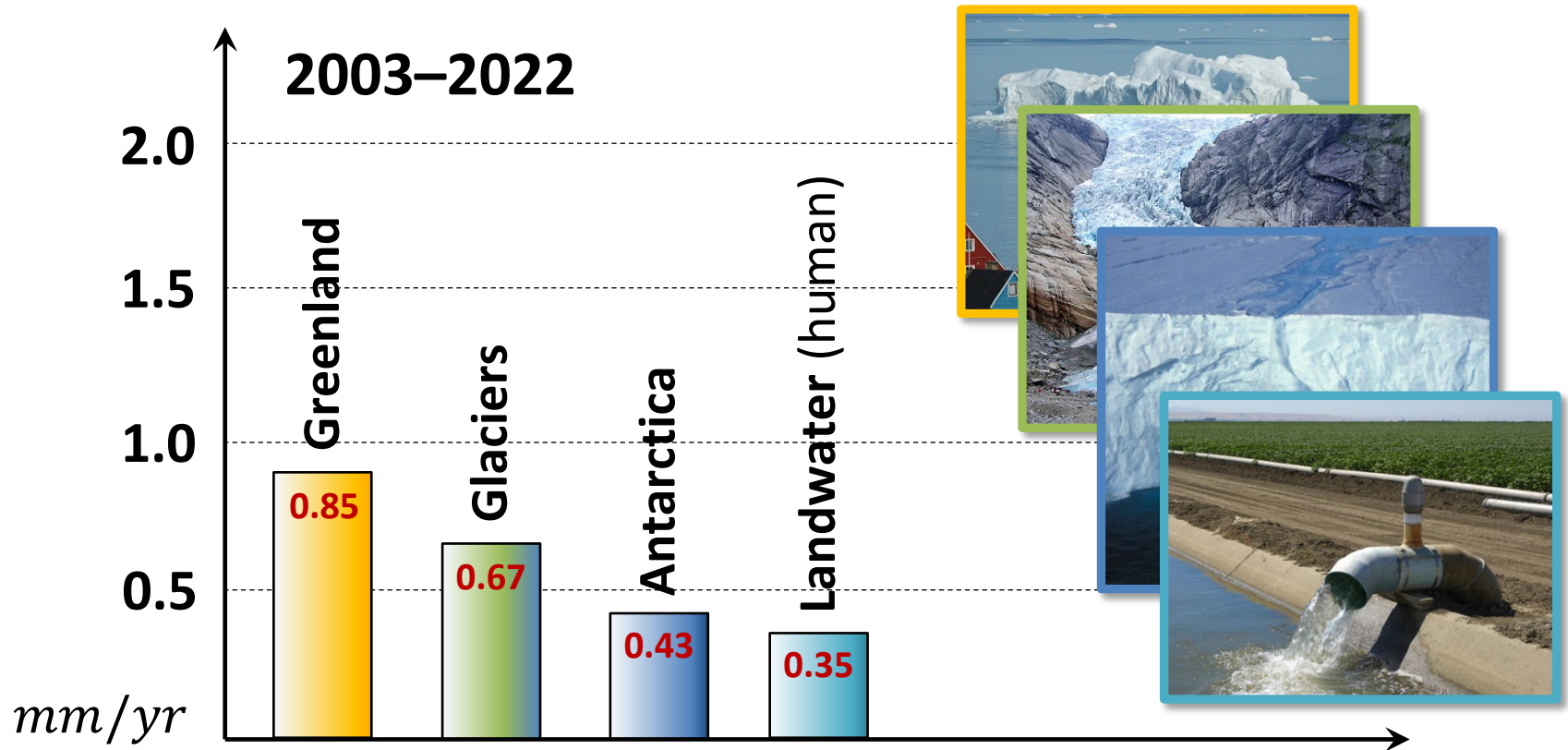
Ludwigsen et al. (2024, Nat. Commun.)

# Basic Considerations

Ludwigsen et al. (2024)

## Global ocean mass budget:

- Trends fitted to time series of individual contributions



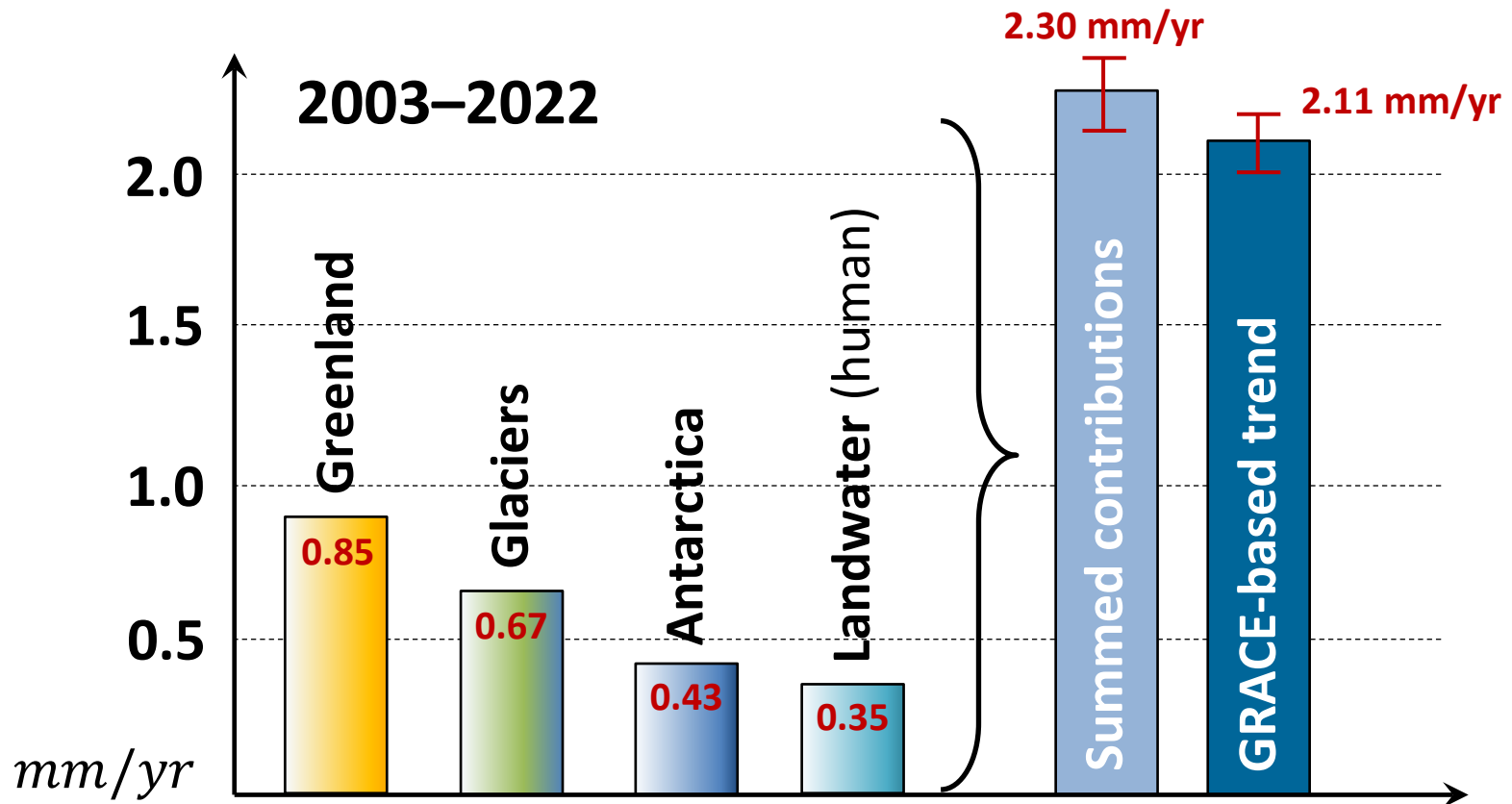


# Basic Considerations

Ludwigsen et al. (2024)

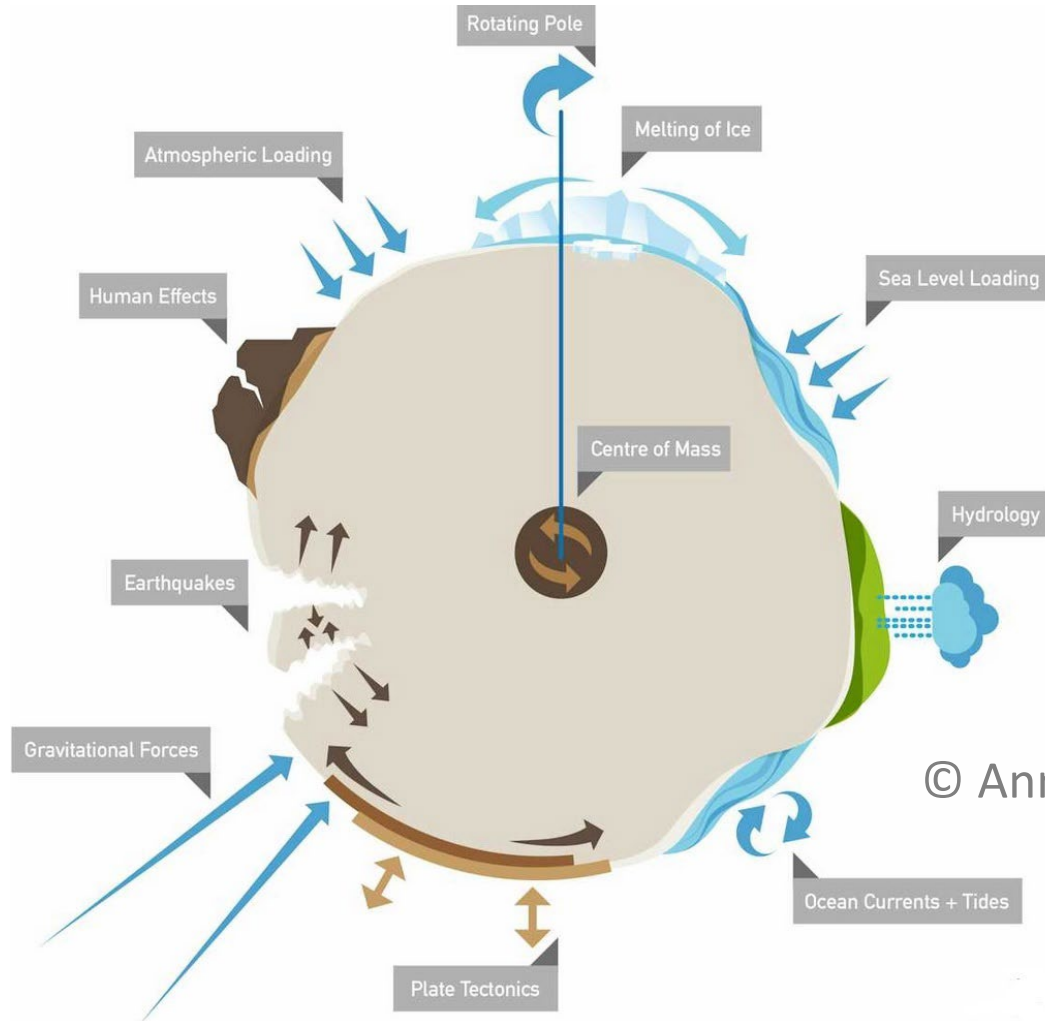
## Global ocean mass budget:

- Trends fitted to time series of individual contributions



# Mass Change of the Oceans

**Bathtub analysis**  $\implies$  **realistic Earth**: includes ...



**G**: Gravitation

**R**: Rotation

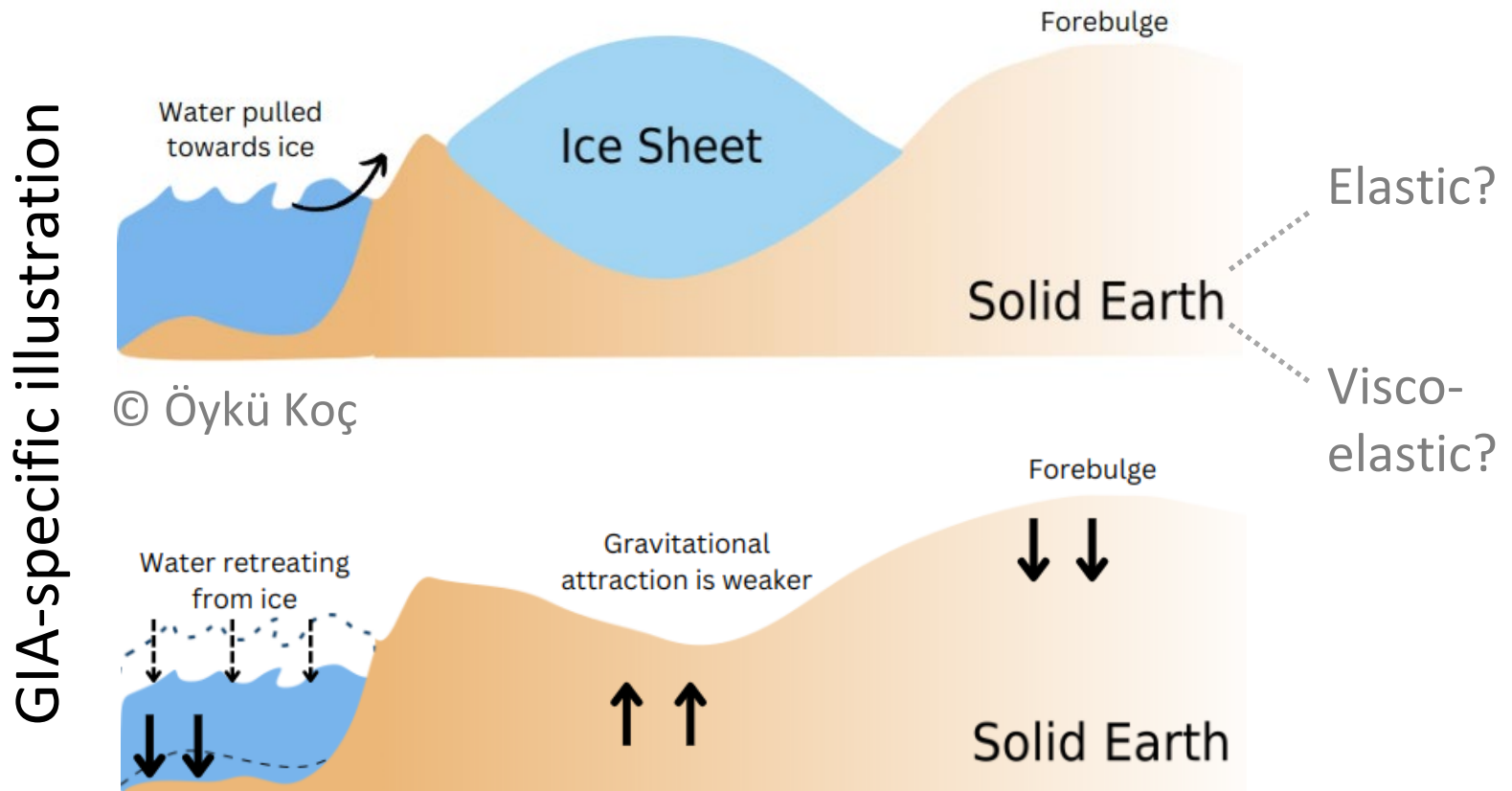
**D**: Deformation

© Anna Riddell

# Land-Ocean Mass Transfer

## Framework of GRD (I):

- Changing surface loads reconfigure sea surface, crust, ...



# Land-Ocean Mass Transfer

## Framework of GRD (II):

- Define mass-conserving loading function

$$\sigma(\theta, \lambda, t) = \underbrace{H(\theta, \lambda, t)C(\theta, \lambda)}_{\text{Change of load on continents with mask } C} + \underbrace{S(\theta, \lambda, t)\mathcal{O}(\theta, \lambda)}_{\text{Associated change in sea level with ocean mask } \mathcal{O}}$$

Change of load on continents with mask  $C$       Associated change in sea level with ocean mask  $\mathcal{O}$

- Compute gravitationally consistent sea level change

$$S(\theta, \lambda, t) = \frac{a}{M} [G(\theta, \lambda) \otimes \sigma(\theta, \lambda, t)] +$$

Rotational feedback + mass conservation constraint

$$+ \frac{1}{g} \sum_{m=0}^2 \hat{\Lambda}_{2m}(t) \hat{Y}(\theta, \lambda)_{2m} + E(t)$$



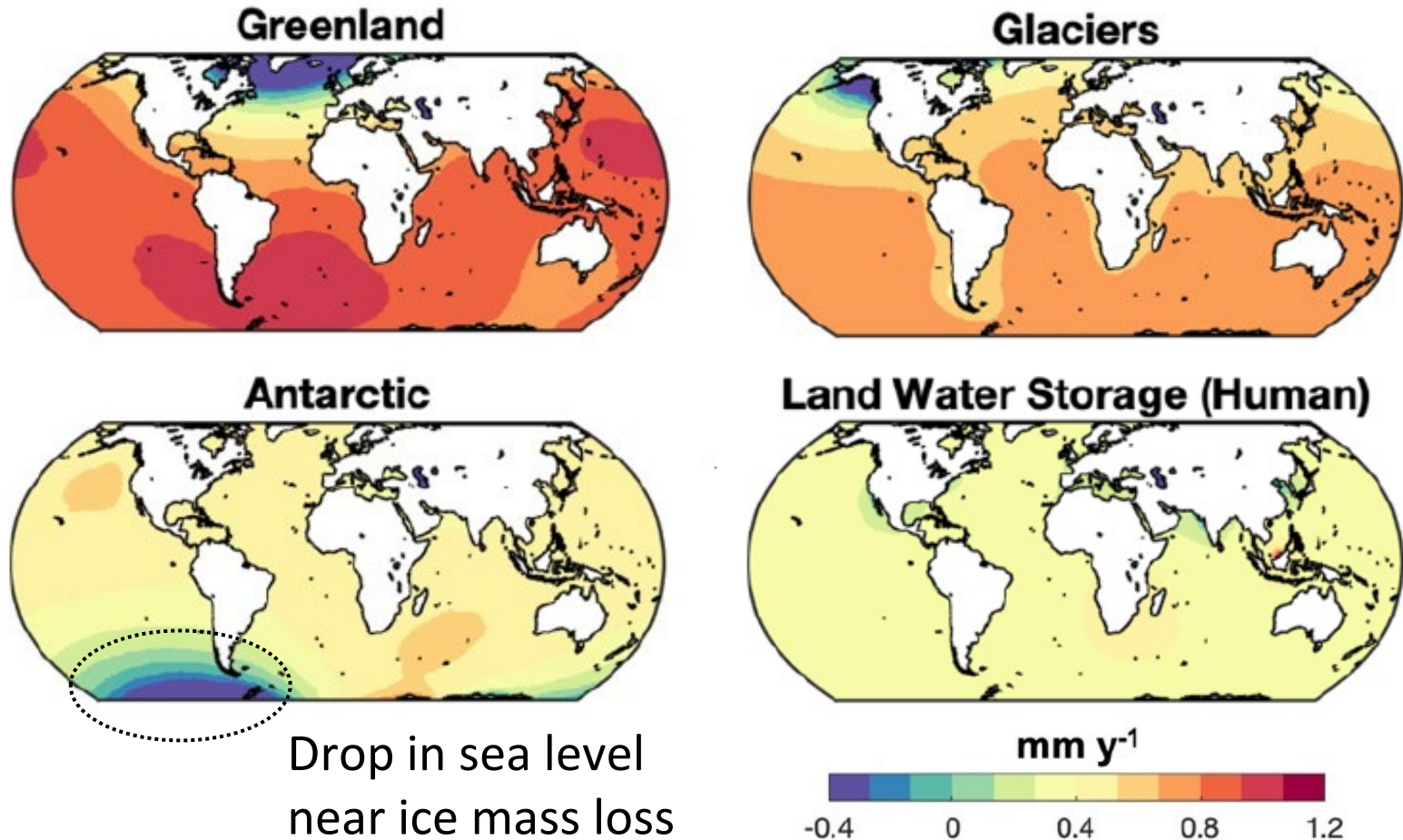
# Land-Ocean Mass Transfer

## Framework of GRD (III):

- Terms and parameters:
  - $a$  ... Earth radius,  $M$  ... total mass of Earth,  $g$  ... gravity acc.
  - $\mathcal{G}(\theta, \lambda)$  ... Green's function that parameterizes the perturbations in the gravitational potential and the associated solid Earth deformation (SED, elastic)
  - $\hat{\Lambda}_{2m}$  ... Degree-2 spherical harmonic coefficients related to perturbations in rotational potential and associated SED
  - $\hat{Y}_{2m}$  ... Degree-2 spherical harmonics, both sine/cosine
  - $E(t)$  ... Eustatic term for mass conservation

# Land-Ocean Mass Transfer

Relative sea level trends (GRD-based): 2003–2022



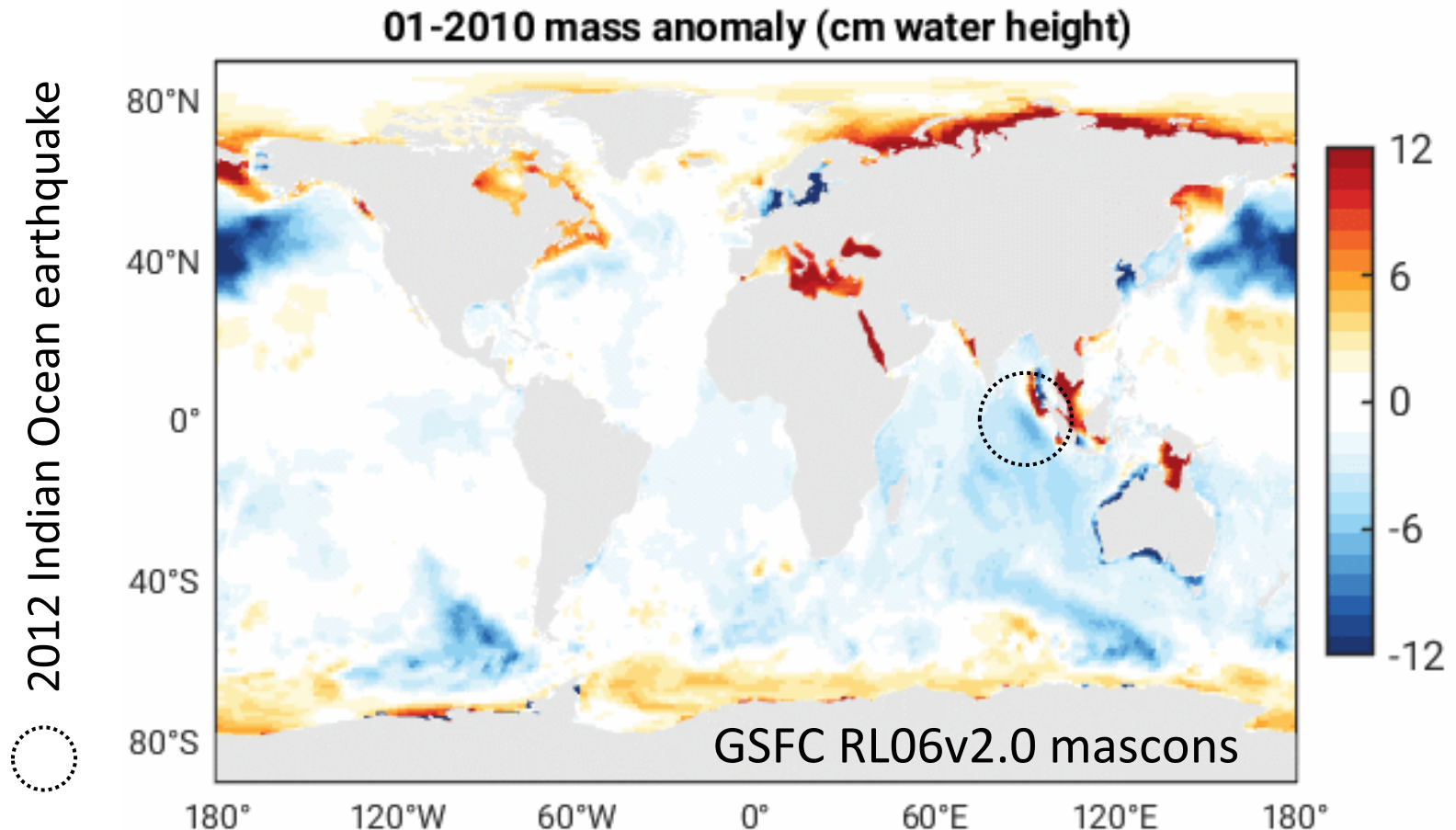
Drop in sea level  
near ice mass loss

Ludwigsen et al. (2024)



# Mass Change of the Oceans

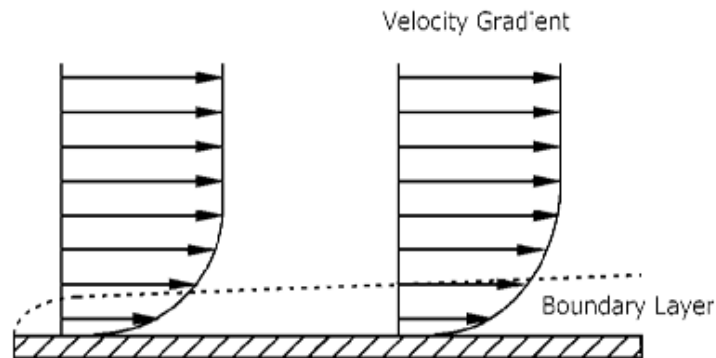
Is this consistent with what GRACE is seeing?



# Mass Change of the Oceans

**What is missing from the picture?**

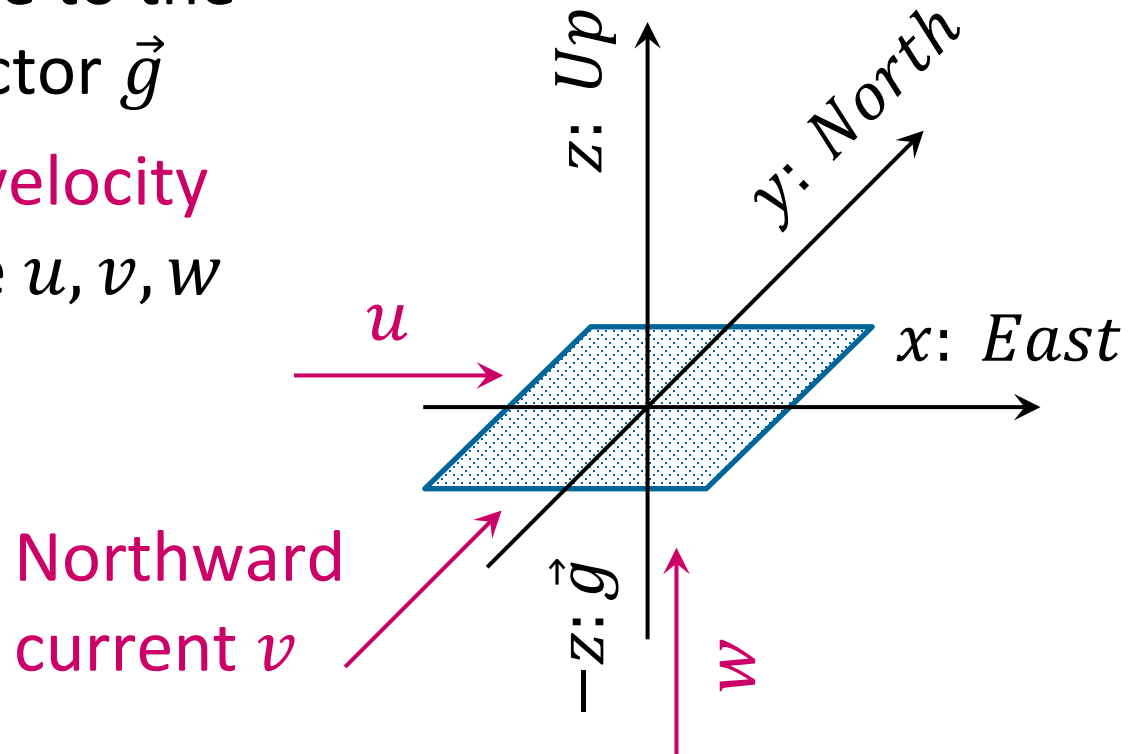
**A: Currents!  $\Rightarrow$  Dynamic ocean**



# Dynamic Ocean

## Coordinate system and some variables:

- „Flat-Earth“, i.e.,  $xy$  plane is a **tangential plane**
- $z$  points opposite to the gravitational vector  $\vec{g}$
- **Corresponding velocity** components are  $u, v, w$

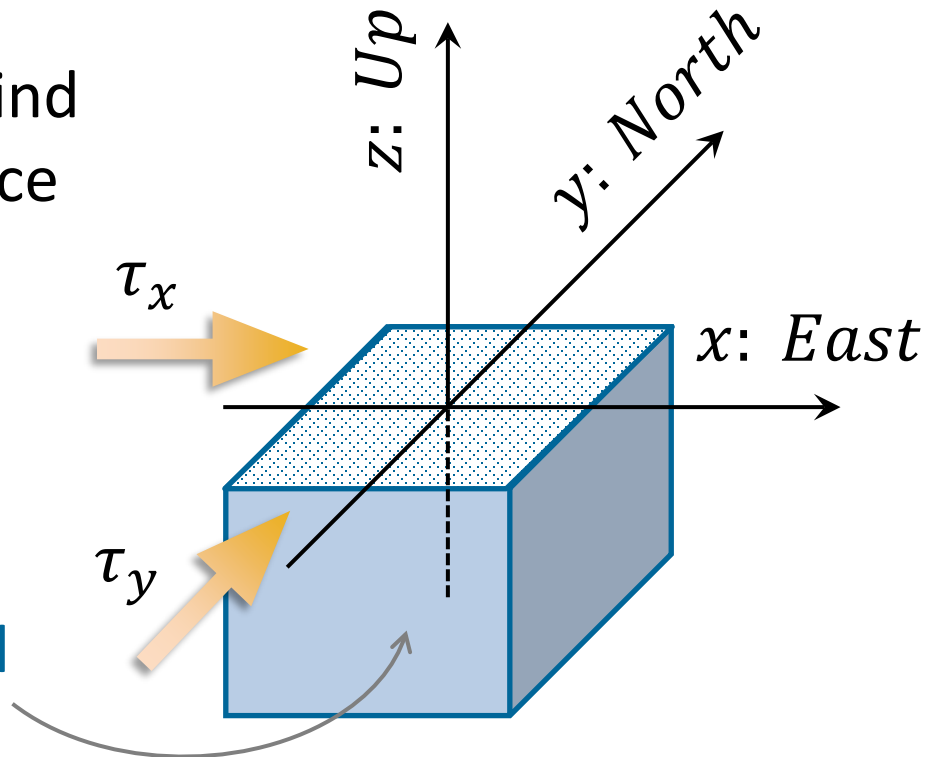


# Dynamic Ocean

## Coordinate system and some variables:

- State variables in 3D: density ( $\rho$ ), **pressure** ( $p$ ), ...
- Also consider **wind stress**:
  - $x, y$  components of wind stress are  $\tau_x, \tau_y$  (= force per unit area  $Nm^{-2}$ )
  - Quadratic in the near-surface wind speed

$\rho, p$  for each parcel



# Dynamic Ocean

Water is set in motion by forces  $F$ :

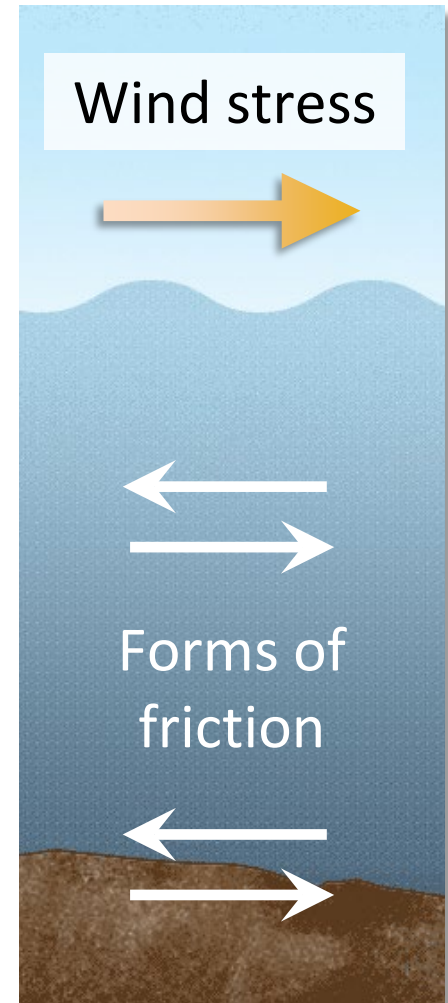
- (1) Pressure gradient
- (2) Coriolis
- (3) Gravity
- (4) Friction

Newton's second law in  $u$  direction:

$$\frac{\partial u}{\partial t} = \frac{1}{m} \sum F$$

*density · particle acceleration =  
= pressure gradient + Coriolis  
+ gravity + friction*

$m \dots$  mass,  $t \dots$  time



# Dynamic Ocean

## Momentum equations – in fuller form:

- The discussed forces balance the acceleration term:

The diagram illustrates the momentum equations for the x, y, and z components of velocity in a fluid. The equations are presented in three rows, with the right-hand side terms grouped into four numbered categories (1, 2, 3, 4) indicated by orange boxes above the terms. A dashed box highlights the pressure gradient and gravity terms in the z-component equation, with a note stating 'Hydrostatic equation appears here'.

$$\frac{\partial u}{\partial t} = \underbrace{-\frac{1}{\rho} \frac{\partial p}{\partial x}}_1 + \underbrace{fv}_2 + \underbrace{-g}_3 + \underbrace{+\frac{1}{\rho} \frac{\partial \tau_x}{\partial z} - Ju}_4$$

$$\frac{\partial v}{\partial t} = \underbrace{-\frac{1}{\rho} \frac{\partial p}{\partial y}}_1 - \underbrace{fu}_2 + \underbrace{+\frac{1}{\rho} \frac{\partial \tau_y}{\partial z} - Jv}_4$$

$$\frac{\partial w}{\partial t} = \underbrace{-\frac{1}{\rho} \frac{\partial p}{\partial z}}_1 - \underbrace{g}_3 - \underbrace{Jw}_4$$

(1) Press. gradient  
 (2) Coriolis  
 (3) Gravity  
 (4) Friction

**Hydrostatic equation** appears here



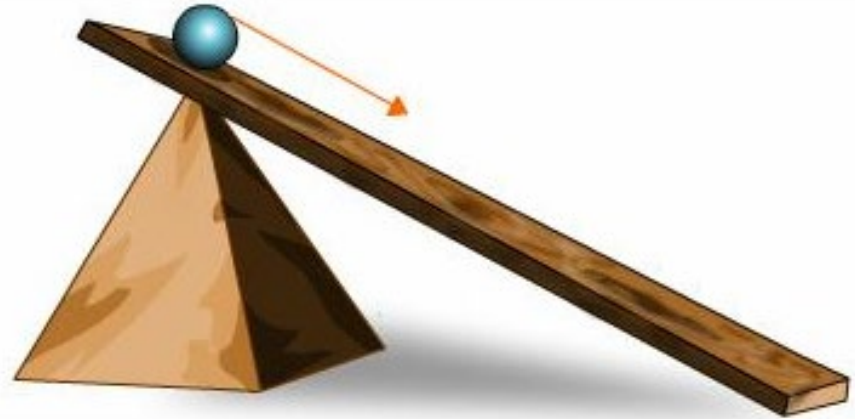
# Dynamic Ocean

## Horizontal **pressure gradient force**:

- Particles move **from high to low pressure**
- Mechanical analogue: ball on frictionless inclined plane

$$\frac{\partial u}{\partial t} = -\frac{1}{\rho} \frac{\partial p}{\partial x}$$

$$\frac{\partial v}{\partial t} = -\frac{1}{\rho} \frac{\partial p}{\partial y}$$



Contribution of  $p$  to equations  
of motion in  $(x, y)$

# Dynamic Ocean

## Coriolis force – general remarks:

- An acceleration occurring when objects are moving ...
- ... in a **non-inertial frame of reference**:
  - Spinning disk
  - Rotating sphere or
  - The local reference frame we adopted (→ slide no. 17)



Earth's angular velocity

Latitude

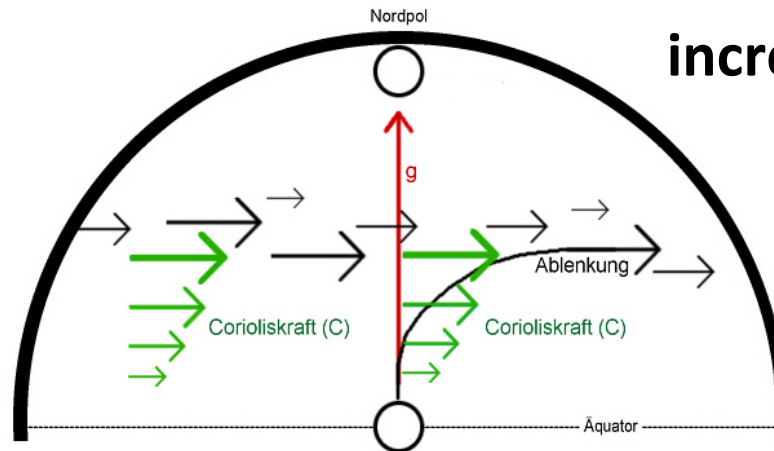
- Coriolis parameter  $f = 2\Omega \sin\varphi$  [ $rad\ s^{-1}$ ]

# Dynamic Ocean

## Coriolis force – basic findings:

Acceleration  
increases with  
increasing latitude

$$\frac{\partial u}{\partial t} = +vf$$
$$\frac{\partial v}{\partial t} = -uf$$



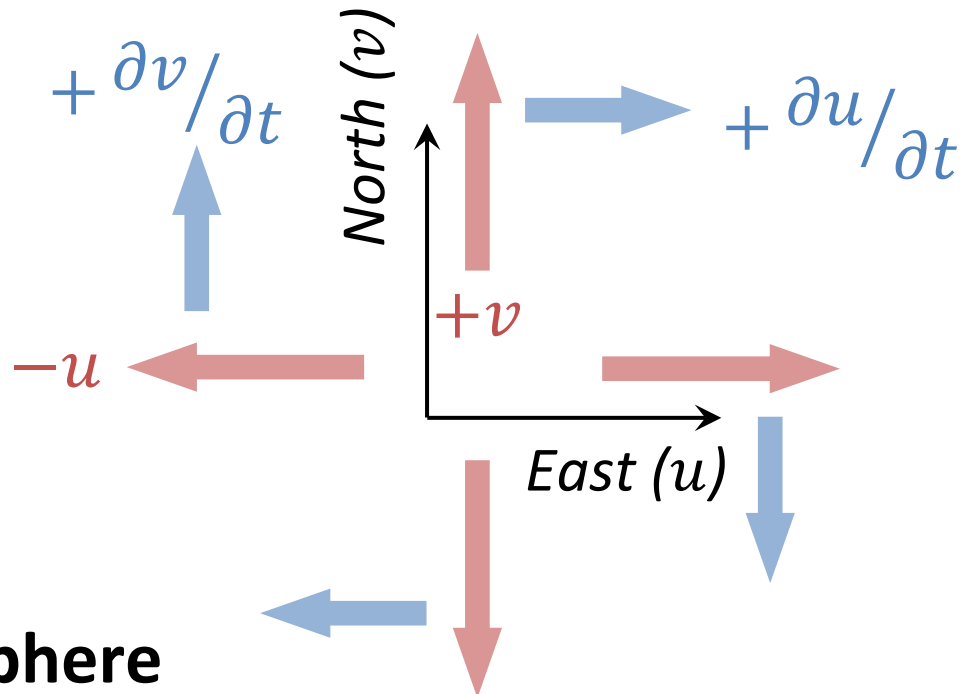
- As  $(u, v)$  are orthogonal, the Coriolis force always acts at right angles to the direction of motion:
  - N-Hemisphere: deflection to the right
  - S-Hemisphere: deflection to left (as  $f$  will be negative)

# Dynamic Ocean

Moving at right angles to the direction of motion:

$$\frac{\partial u}{\partial t} = +vf$$

$$\frac{\partial v}{\partial t} = -uf$$



- Picture in **N-Hemisphere**
- Motion in  $v$  direction triggers deflection in  $u$  direction
- Particles will follow a clockwise path in this case

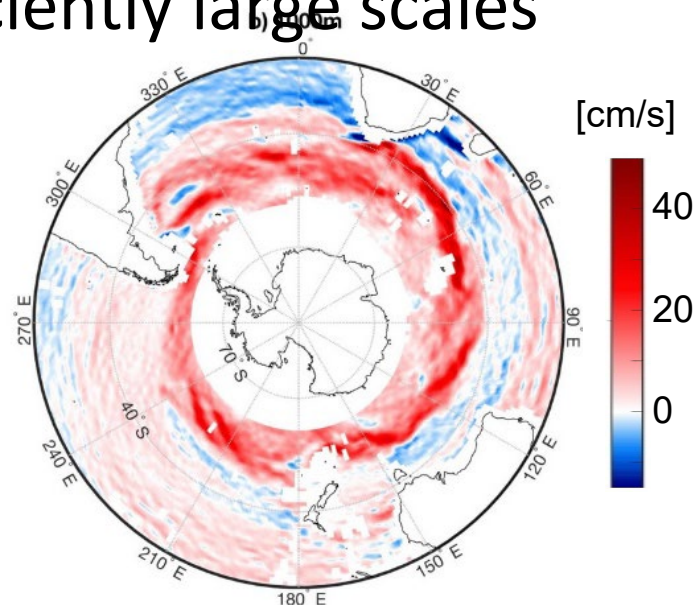
# Dynamic Ocean

## Subsetting the momentum equations:

- Assume that all currents are horizontal and steady-state
- No wind stress is acting and friction is negligible
- Processes of interest have sufficiently large scales

$$\frac{\partial u}{\partial t} = -\frac{1}{\rho} \frac{\partial p}{\partial x} + fv + \frac{1}{\rho} \frac{\partial \tau_x}{\partial z} - Ju$$

$$\frac{\partial v}{\partial t} = -\frac{1}{\rho} \frac{\partial p}{\partial y} - fu + \frac{1}{\rho} \frac{\partial \tau_y}{\partial z} - Jv$$



# Dynamic Ocean

Result = **Geostrophic equation:**

- The momentum equations are reduced to a simple balance relationship between the ...
- **Pressure force** and the **Coriolis accelerations** (l.h.s.)

$$fv = \frac{1}{\rho} \frac{\partial p}{\partial x}$$

$$fu = -\frac{1}{\rho} \frac{\partial p}{\partial y}$$

- $(u, v)$  are geostrophic currents
- Forces involved very small, but still largest in the ocean's interior
- Good approximation for *Gulf Stream*, *Antarctic Circumpolar Current (ACC)*, etc.



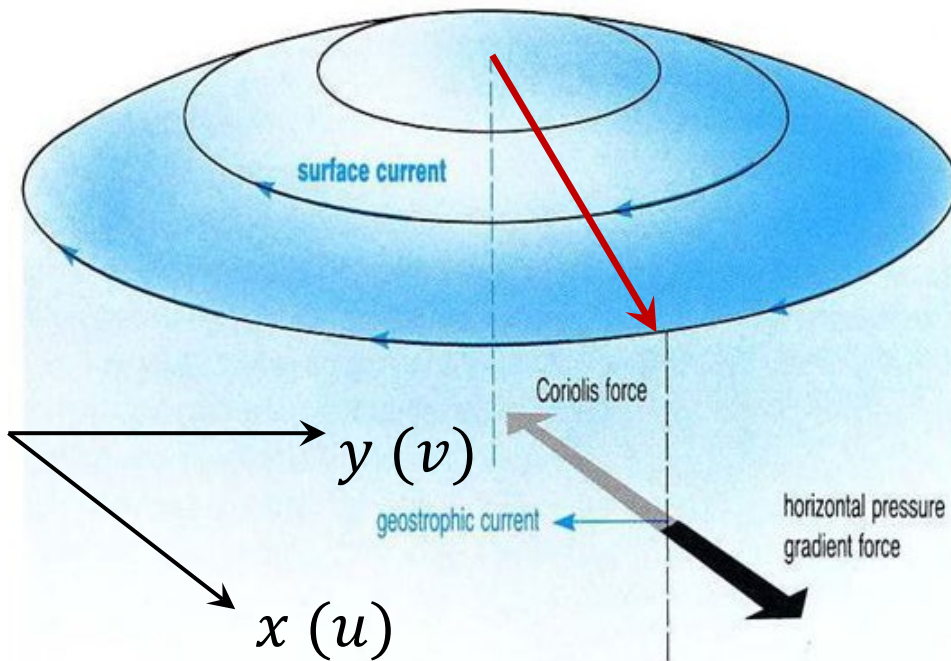
# Dynamic Ocean

## Consequences of the geostrophic equation:

Elevated pressure  
surface **N-Hemisphere**

$$fv = \frac{1}{\rho} \frac{\partial p}{\partial x}$$

$$fu = -\frac{1}{\rho} \frac{\partial p}{\partial y}$$

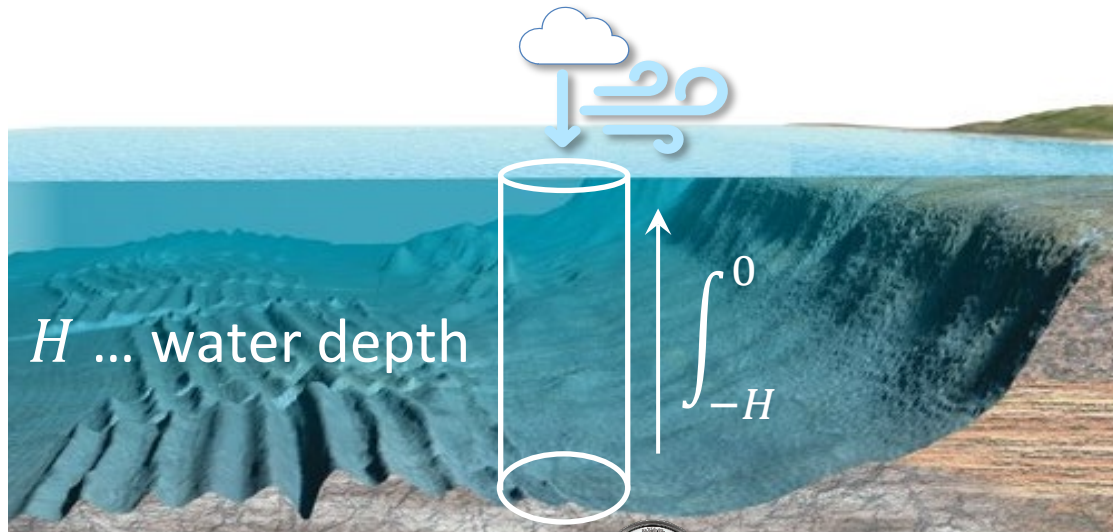


- $\partial p / \partial x$  is negative in this configuration
- With  $f > 0$ , a negative  $v$  current follows
- **Clockwise motion** in N-Hemisphere

# Mass Change of the Oceans



**OBP = Ocean Bottom Pressure ( $\rightarrow$  mass)**



$H$  ... water depth

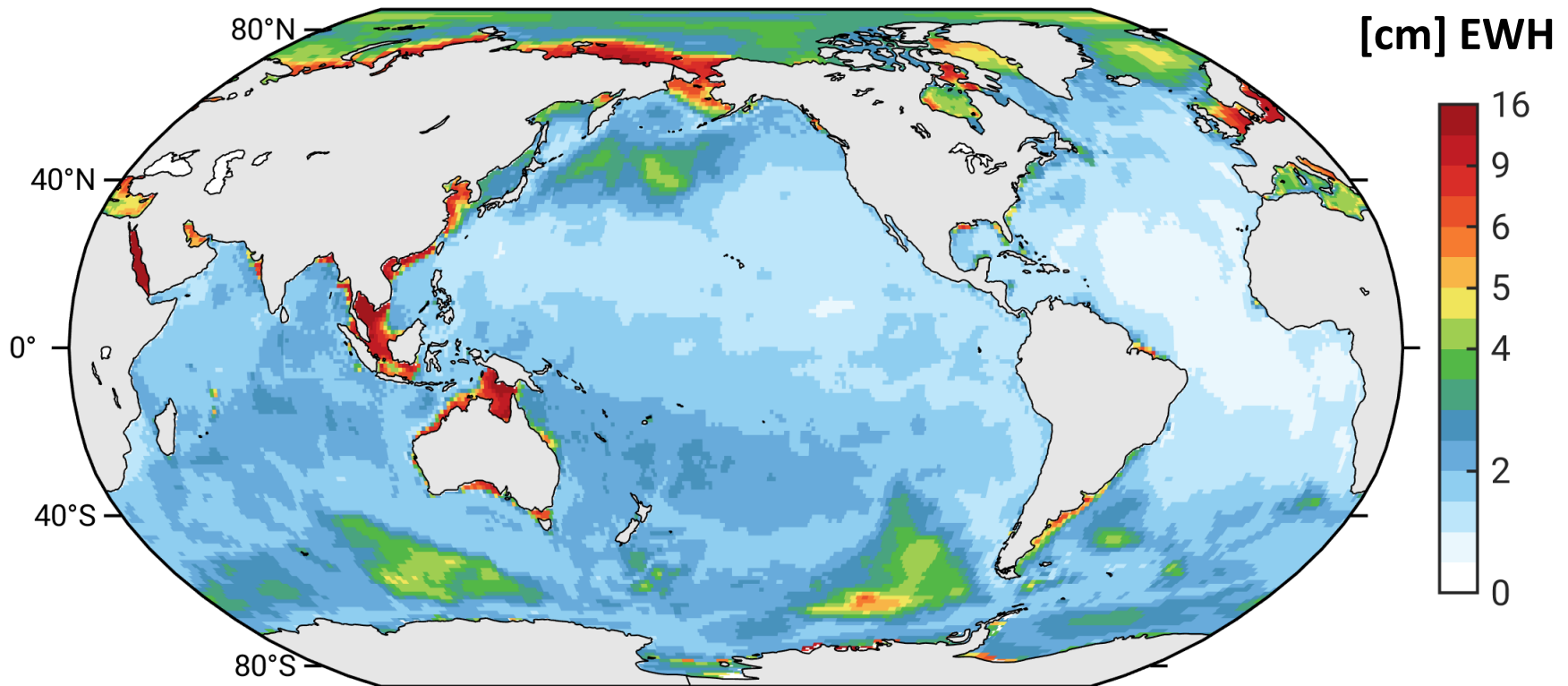
Weight of overlying fluid column  $\uparrow$



# Ocean Bottom Pressure

## Global view of observed OBP signals:

- $\sigma$  of anomalies (spatial mean & trend reduced)



# Ocean Bottom Pressure

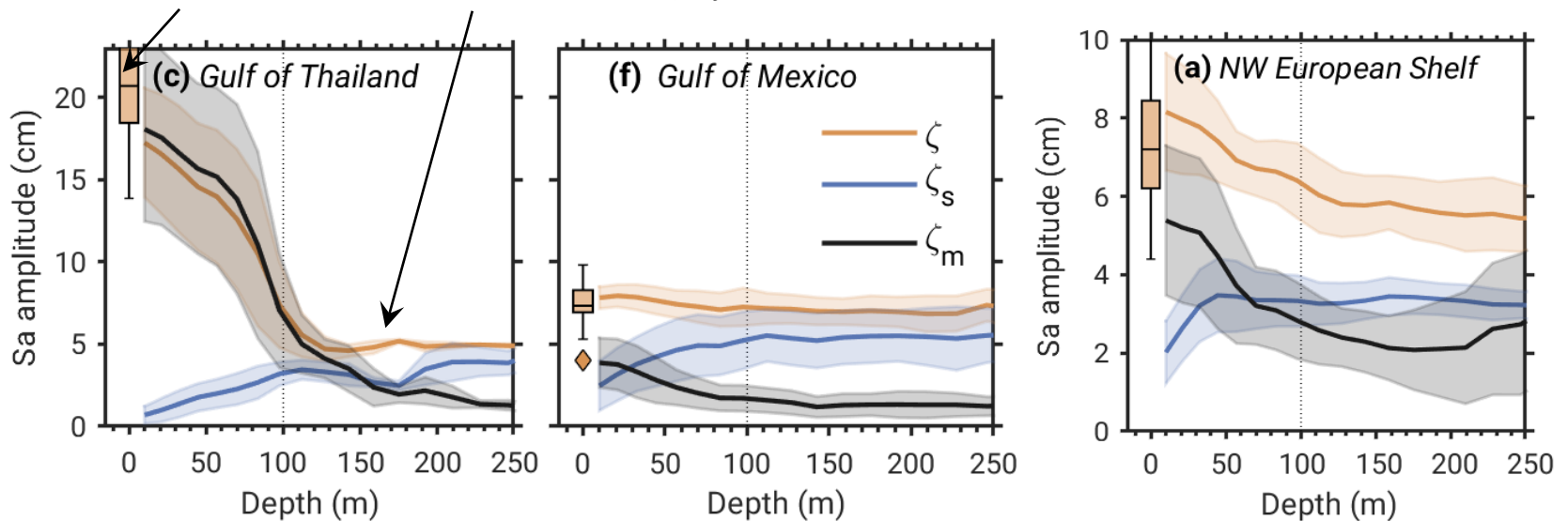
## GRACE/-FO & ocean applications (I):

- Partitioning of sea level ( $\zeta$ ) variability
  - **Manometric** ( $\zeta_m$ ) vs. **steric** ( $\zeta_s$ ) variability:  $\zeta = \zeta_m + \zeta_s$
  - E.g., for annual cycle, plotted over depth

$\zeta$ : Tide gauges, altimetry

$\zeta_m$ : GRACE/-FO

$\zeta_s$ : Hydrographic profiles

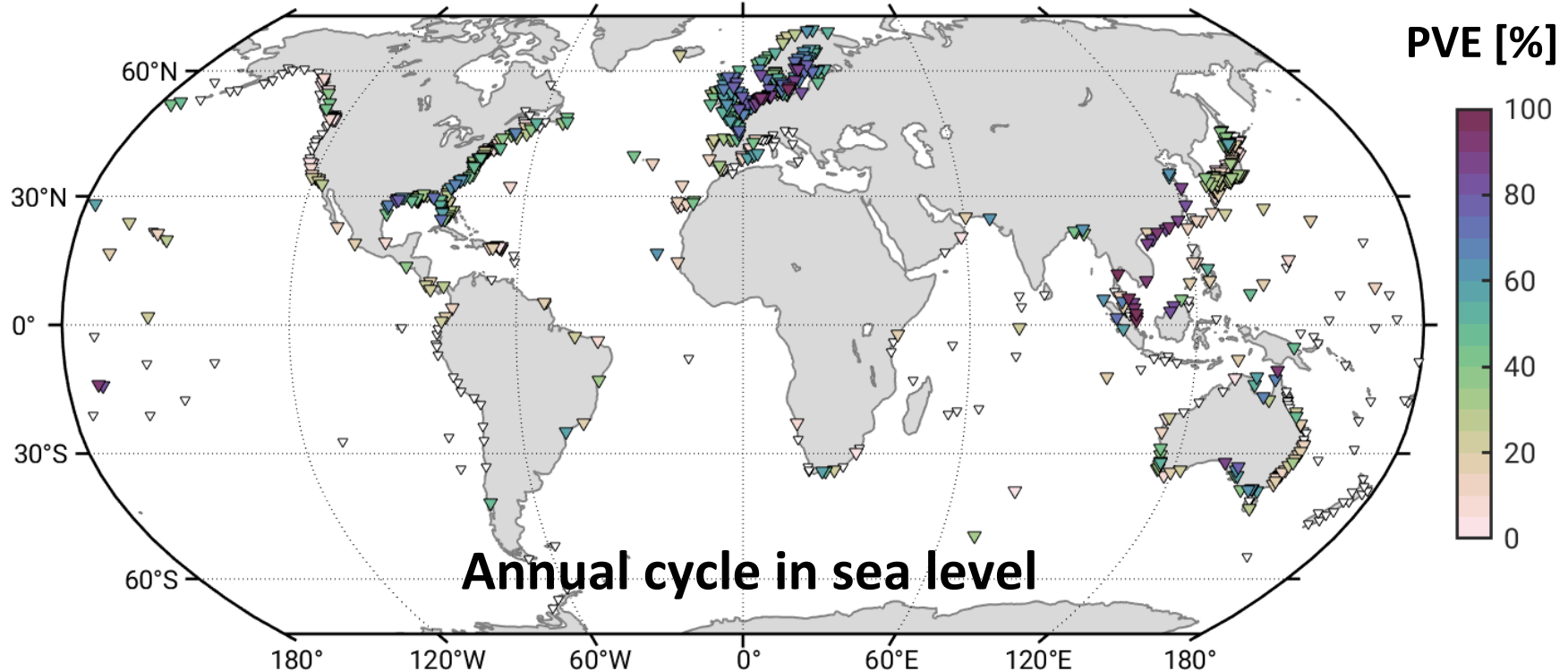


# Ocean Bottom Pressure

## GRACE/-FO & ocean applications (I):

- $\zeta_m$  explains how much variance in coastal sea level?

Ponte & Schindelegger (2024, Earth Space Sci.)

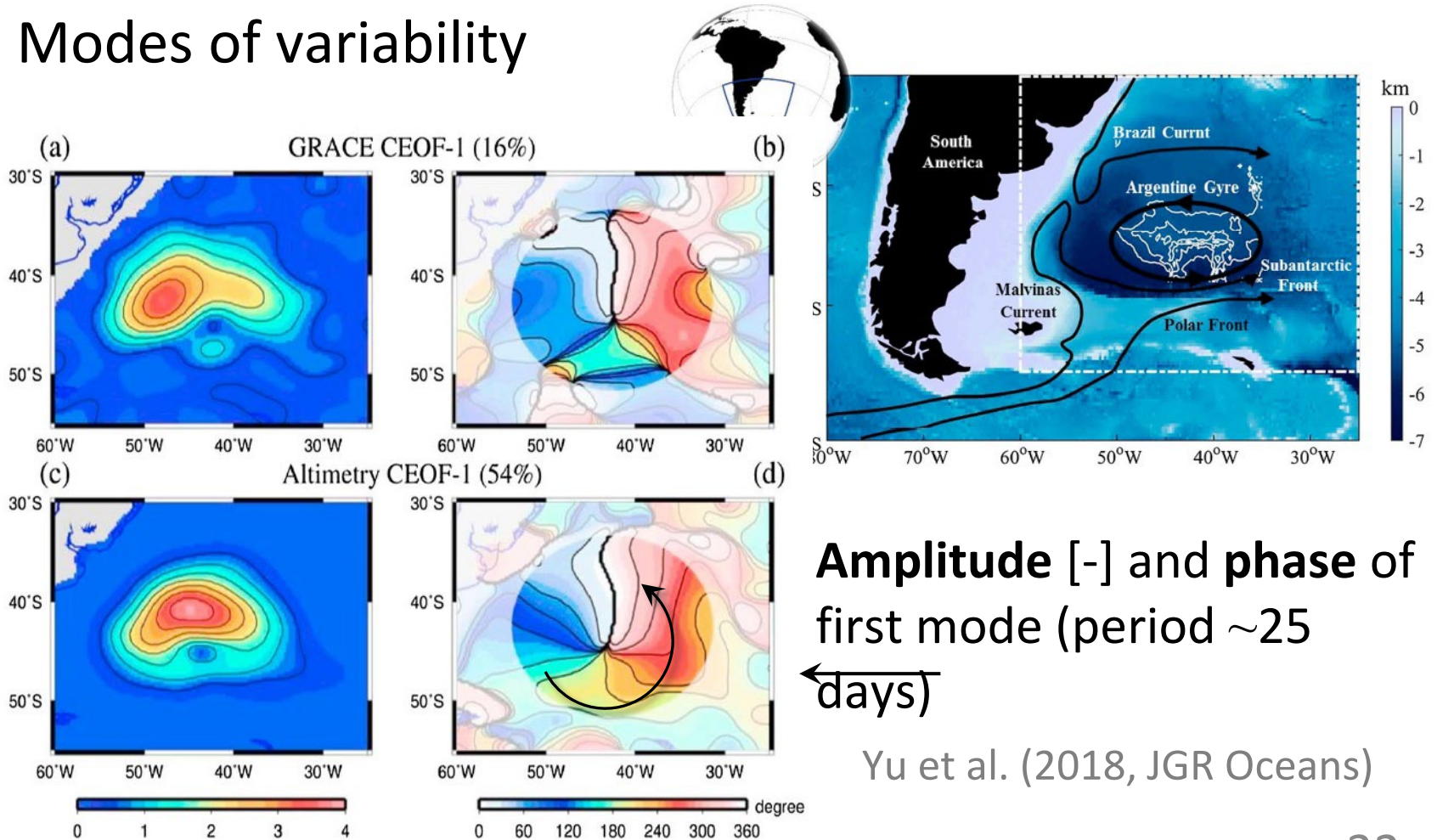




# Ocean Bottom Pressure

## GRACE/-FO & ocean applications (II):

- Modes of variability



# Ocean Bottom Pressure

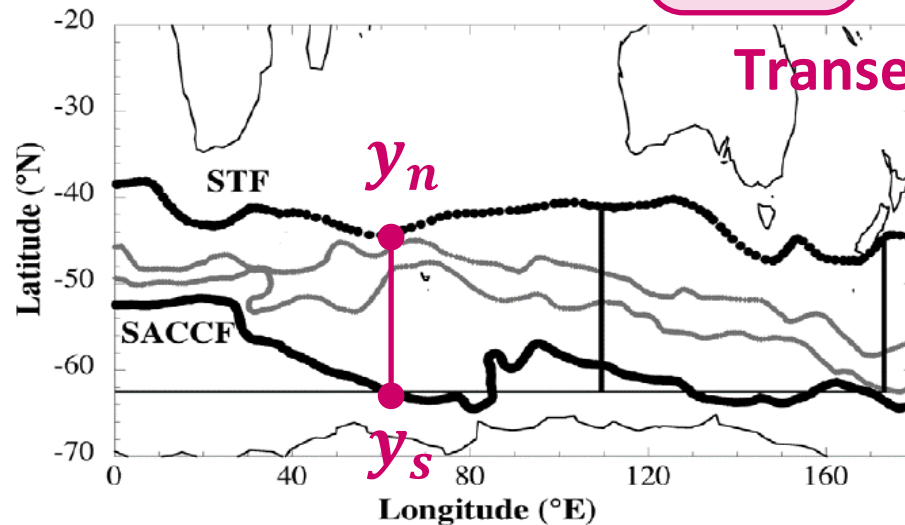
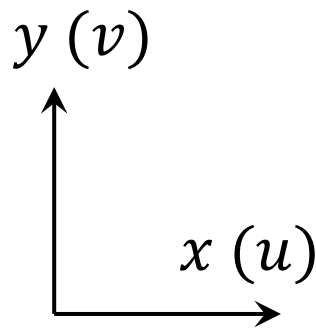
## GRACE/-FO & ocean applications (III):

- Transport variability  $\Delta T$  from geostrophy

Bottom current

OBP anomaly

$$fu = -\frac{1}{\rho} \frac{\partial p}{\partial y} \Rightarrow \Delta T(x) = - \int_{y_s}^{y_n} \int_{-H}^0 \frac{1}{f\rho} \frac{\partial p}{\partial y} dz dy$$



Transect integral

# Ocean Bottom Pressure

## GRACE/-FO & ocean applications (III):

- Transport variability  $\Delta T$  from geostrophy

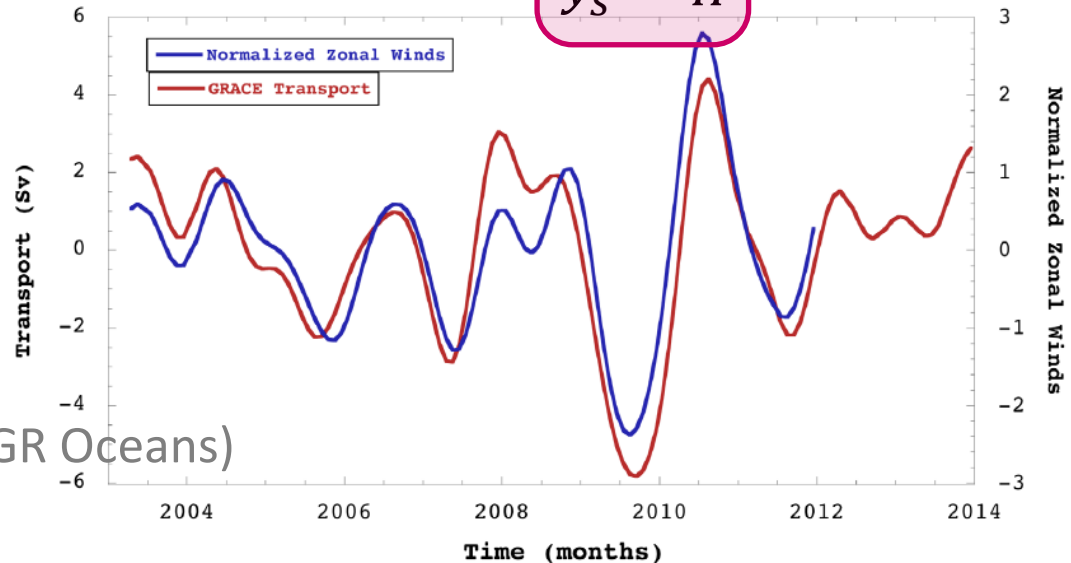
Bottom current

OBP anomaly

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**ACC transport variability at 60°E**

Makowski et al. (2015, JGR Oceans)

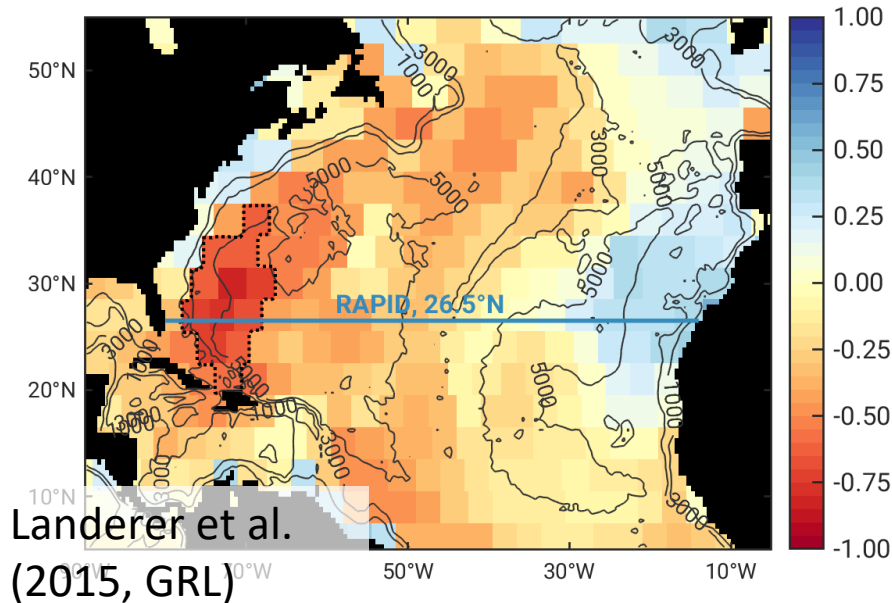




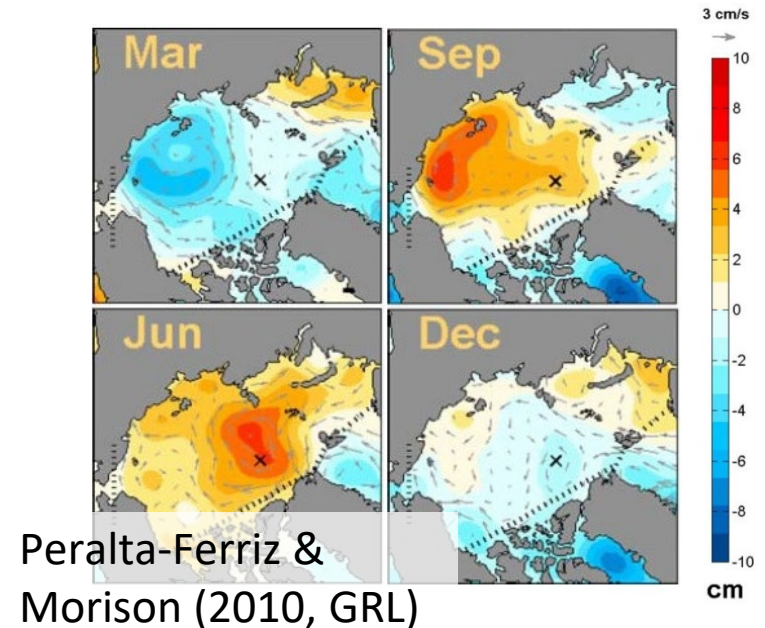
# Ocean Bottom Pressure

## GRACE/-FO & ocean applications (III):

- $\Delta T$  or currents from geostrophy – other examples



Correlation OBP  $\leftrightarrow$  GRACE-derived transport at 26.5°N

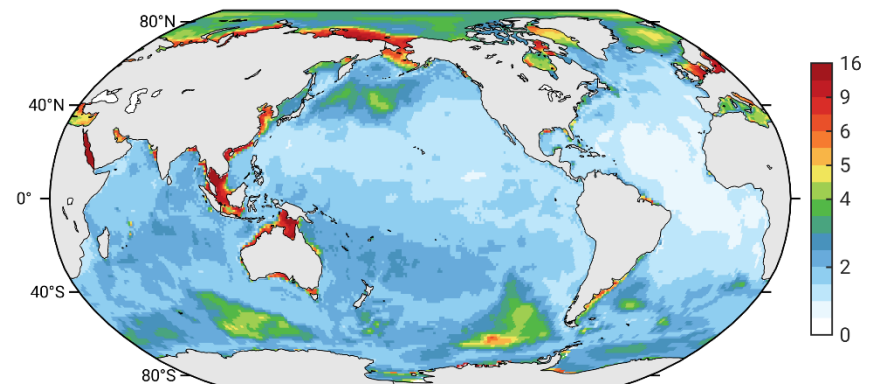
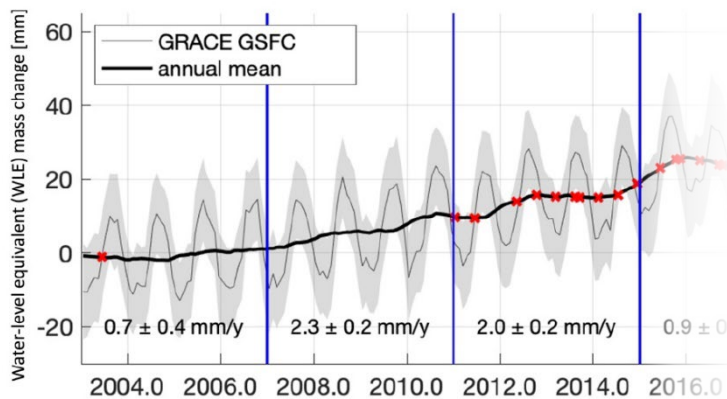


Arctic OBP (cm) and resulting geostrophic velocity ( $\rightarrow$ )

# Mass Change of the Oceans

## Take-away messages:

- Mass change of the ocean is an interdisciplinary topic
- Multiple facets and spatiotemporal scales:
  - Global ocean mass → climate, gravity & deformation
  - Local to regional variability → dynamics
- Key insights from satellite gravimetry



# Mass Change of the Oceans

## References:

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